## Cartoon time courtesy of the ? view of tree space



## Parsimony-informative Pattern Frequency Space

P(1100)


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$P(1100)$


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$P(1100)$


## Pattern Frequency Space With Observed Data



## ML scores in Pattern Frequency Space

P(1100)
$\ln L\left(T_{1} \mid X\right)=-D_{K L}\left(f_{X} \mid f_{T_{1}}\right)$

LR statistics in Pattern Frequency Space
P(1100)
Black is $\ln L\left(T_{A B}\right)-\ln L\left(T_{A C}\right)$

## KH Test in Pattern Frequency Space

P(1100)
Uses the $\delta$ test statistic and a null distribution centered on the boundary

## Parametric bootstrapping in Pattern Frequency Space

$P(1100)$
Uses the $\delta$ test statistic and a null distribution centered on point that arises from the best tree in $H_{0}$


Susko modification to param. boot.:
Uses the $\delta$ test statistic and a null distribution centered on point that arises from the best tree in $H_{0}$ but with branches in conflict with $\hat{T}$ constrained. to be 0 .

P(1100)


P(1010)
P(1001)

Efron et al. (1996) view of tree space


## Parsimony-informative Pattern Frequency Space

P(1100)


Imagine hypothesis tests of locations with different border shapes:


Similar dataset with point estimates (red dot) in $H_{1}$
Green dot is the hardest set of locations in $H_{0}$ to reject.


Non-parametric Bootstrapping in Pattern Frequency Space


## Bootstrapping in Pattern Frequency Space (if you had more data)

## P(1100)

AU Test uses multiple sequence lengths to correct BP for any curvature in the boundary between trees


## aBP in Pattern Frequency Space

Null distribution for BP
is calculated using
Normal approximations from polytomy

P(1100)

$\mathrm{P}(1010)$
P(1001)

## aLRT and aBayes in Pattern Frequency Space

$\mathrm{P}(1100)$
In aLRT, we use mixtures of $\chi^{2}$ and selection bias corrections to calculate the $P$-value.


In aBayes, we normalize the ML scores to sum to 1

## References

Efron, B., Halloran, E., and Holmes, S. (1996). Bootstrap confidence levels for phylogenetic trees. Proceedings of the National Academy of Science, U. S. A., 93:13429-13434.

