

Homework #3

(due Monday, Feb 25th)

(1) A snail species has two different morphs, left-coiled and right-coiled. A researcher does a large experiment measuring the escape behavior of snails when confronted with a predator. She classifies each as 'run' or 'hide' (pull into shell). 50% of the snail population exhibit the run behavior. Among runners, 25% are left-coiled. Among hidiers, 60% are left-coiled. Calculate the probability that a snail runs given that it is right-coiled.

(2) Let's revisit the analysis of data on the number of substitutions on two branches of a genealogy, where the two branches have the same time to the most recent common ancestor. We'll denote the data on counts of the number of changes is y_1 and y_2 . Previously JKK worked through the case of using a Poisson distribution with an expectation of ut as a model for these data. He only used the number of sites with differences.

Now imagine that we know the number of sites that we have sequence from. Call that total M . Since mutations are rare M is typically much larger than $y_1 + y_2$. If we imagine that mutations are rare independent events that happen with the same rate at every site, then we can view the data on y_1 and y_2 as given M sites as samples from the binomial distribution. Let p be the probability of a change at one site on a single branch.

- (a) What is the likelihood equation for p given y_1 , y_2 , and M trials?
- (c) What is the formula for the MLE, \hat{p} ?
- (c) What is the MLE of p if $y_1 = 2$, $y_2 = 3$, and $M = 2000$?
- (d) What is the log-likelihood at that point?
- (e) Can you reject a null hypothesis that $p = 0.001$? (show the LRT test statistic and df)

(3) If you knew exactly where in the sequence of 2000 sites the 5 changes occurred, then you could calculate the probability without the binomial coefficient instead of the one you used in #2b. If you used a likelihood equation without the binomial coefficient, you would get a (Circle one answer for each part):

- (a) LOWER / EQUAL / HIGHER likelihood
- (b) LOWER / EQUAL / HIGHER log-likelihood
- (c) LOWER / EQUAL / HIGHER estimate of \hat{p}
- (d) LOWER / EQUAL / HIGHER LRT for the H_0 that $p = 0.001$

(compared to the values of these entities when you use a likelihood equation with the binomial coefficient).